



# Real-Life DOE\*

## Using Graphical Diagnostics to Deal with Bad Experimental Data\*\*

\* Slides posted at [www.statease.com/webinar.html](http://www.statease.com/webinar.html)

*Communication issues: To avoid disrupting the audio, we must mute all for these worldwide webinars. It will best if you email questions to my attention via [stathelp@statease.com](mailto:stathelp@statease.com). However, at intervals we will look for any entered live in the GotoWebinar screen. If we cannot answer immediately, please accept our apology in advance. Then bear with us by repeating your question via email afterwards. We would like to hear from you! -- Mark*



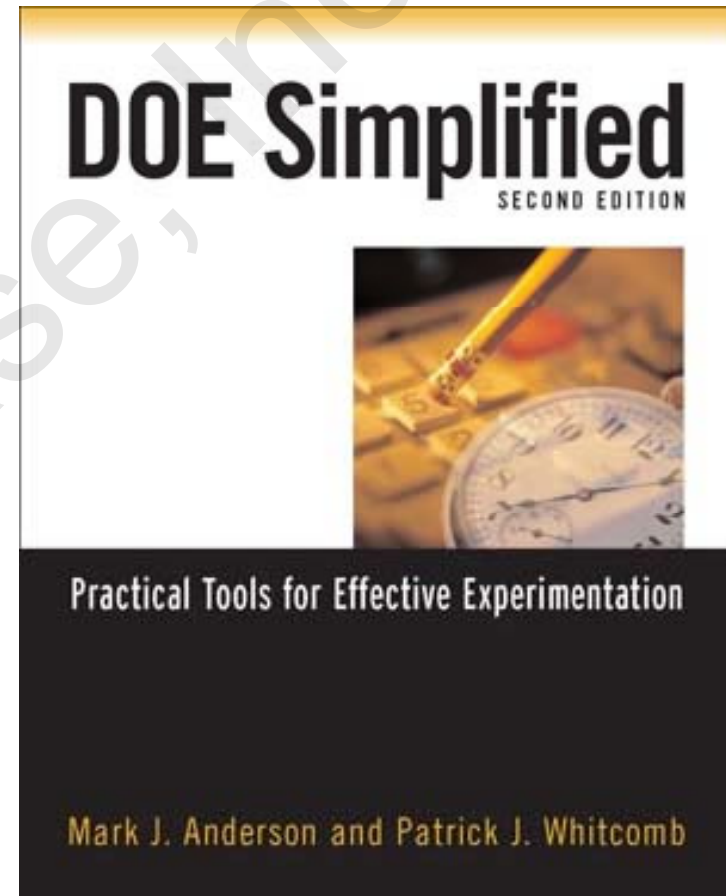
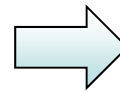
By Mark J. Anderson, PE, CQE  
Stat-Ease, Inc., Minneapolis, MN  
[mark@statease.com](mailto:mark@statease.com)

\*\* Re Anderson & Whitcomb, *Quality Engineering*, April-June 2007, Vol 19, No 2

*Now in 2<sup>nd</sup> edition\*!*

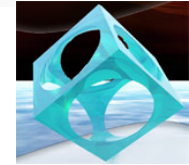
*Web-Based 'Launch Pad'*  
(Chapters 1-3)

Presenter: Demo Sect 1-2 with PIP via  
<http://statease.info/DOEpresentations/>



*\* Productivity Press (CRC, Taylor & Francis) New York, 2007.*

## Mission for this Webinar



### Objective:

Keeping things relatively simple\* statistically (KISS) provide some tricks of the trade that salvaged outstanding results from actual experiments.

\* (Some may disagree due to bits of math & trig.  
Warning: arc-sine square-root ahead.)



- ❑ Thorny issues (stuff happens)
- ❑ The secret to long life (bearing case)
- ❑ A case to test your metal (defects defeated!)
- ❑ Conclusions

# Thorny Issues! (1 of 2)

How to maintain reasonable balance between two types of errors:

1. Focusing on data that vary only due to **common causes**, thus introducing **bias**. (False Positive.)

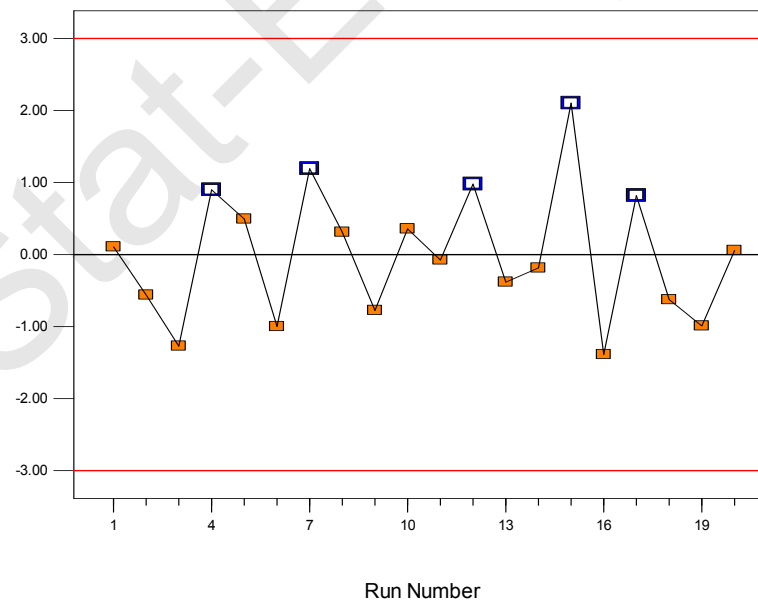
*Examples:*

*+ cold fusion [keeping only the highs],*

*– Pig's Eye treatment [keeping only the lows].\**



Real-Life DOE



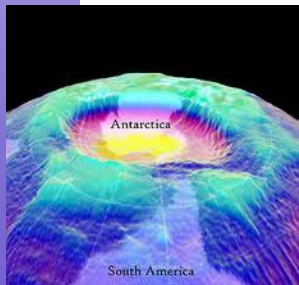
\*Source:  
James J. Anderson  
—Mark's father.

# Thorny Issues! (2 of 2)

How to maintain reasonable balance between two types of errors:

2. Overlooking true (**special cause**) outlier(s)  
(False Negative.) Thus:

- Obscuring real effects (*case later*) or
- Drawing false conclusions and/or
- Losing chance in future to:
  - ✓ Prevent failure (*ex. ozone hole\**) or
  - ✓ Reproduce breakthrough improvements ('Eurekas' such as 3M Postit Notes®).



Real-Life DOE

*\*"When the first measurements were taken the drop in ozone levels in the stratosphere was so dramatic that at first the scientists thought their instruments were faulty."  
- <http://www.theozonehole.com/ozoneholehistory.htm>*

# "Stuff" Happens!

- Typographical errors (*suggestion: type data from top, proof from bottom*)
- Breakdowns in equipment
- Mistakes by operators\*
- Non-representative samples
- Bad measurements
- Unknown lurking variables that appear only intermittently



*Has any stuff like this ever happened to you?*

\*(Defending champion Tony Stewart triggered a chaotic crash at Talladega Superspeedway collected 10 of the 12 title contenders in an October 2012 NASCAR race.)

## It could be worse!



*Mark,*

*Good Afternoon, I appreciate you calling me and discussing the results. We had an accident in the lab and one of the techs caught on fire.*

*-Myra*



# Two Types of Error

*Stuff does not always happen!*

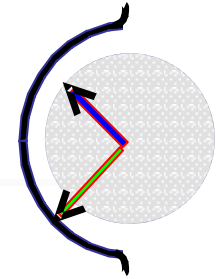
Outliers(s)?		What you say:	
		Yes	No
The truth:	Yes	Correct	2. False Negative
	No	1. False Positive	Correct

*Let's look at two case studies illustrating both errors.*

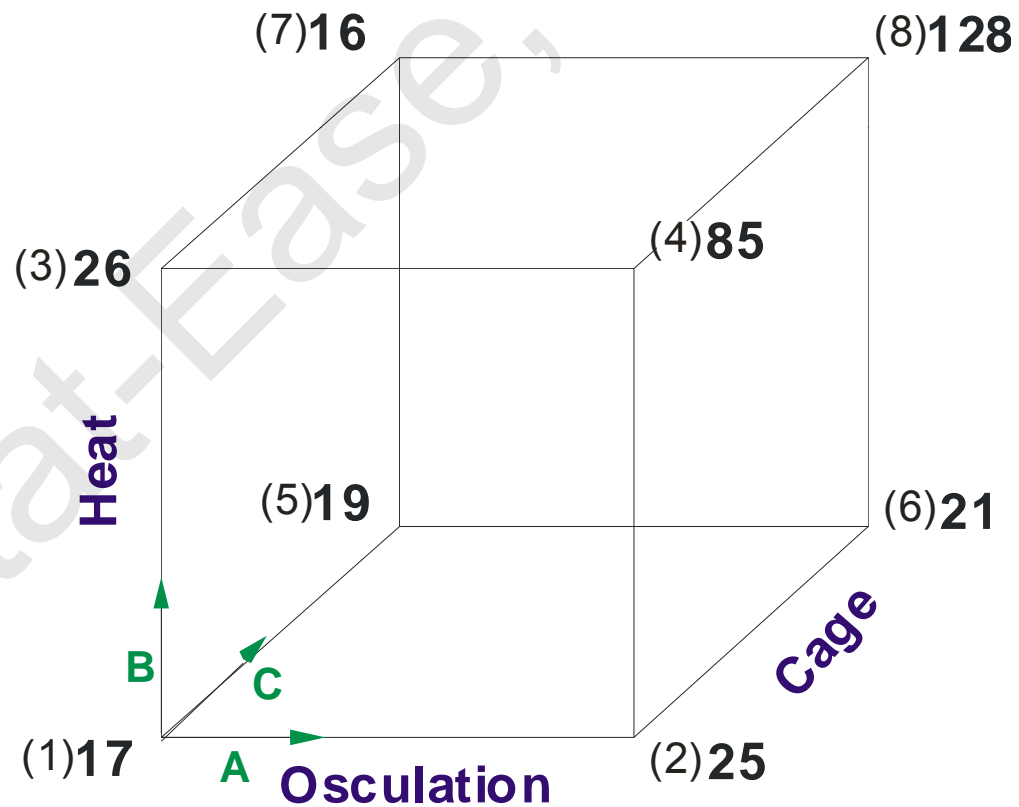


- ✓ *Thorny issues (stuff happens)*
- ❑ The secret to long life (bearing case)
- ❑ A case to test your metal (defects defeated!)
- ❑ Conclusions

# THE SECRET TO LONG LIFE!

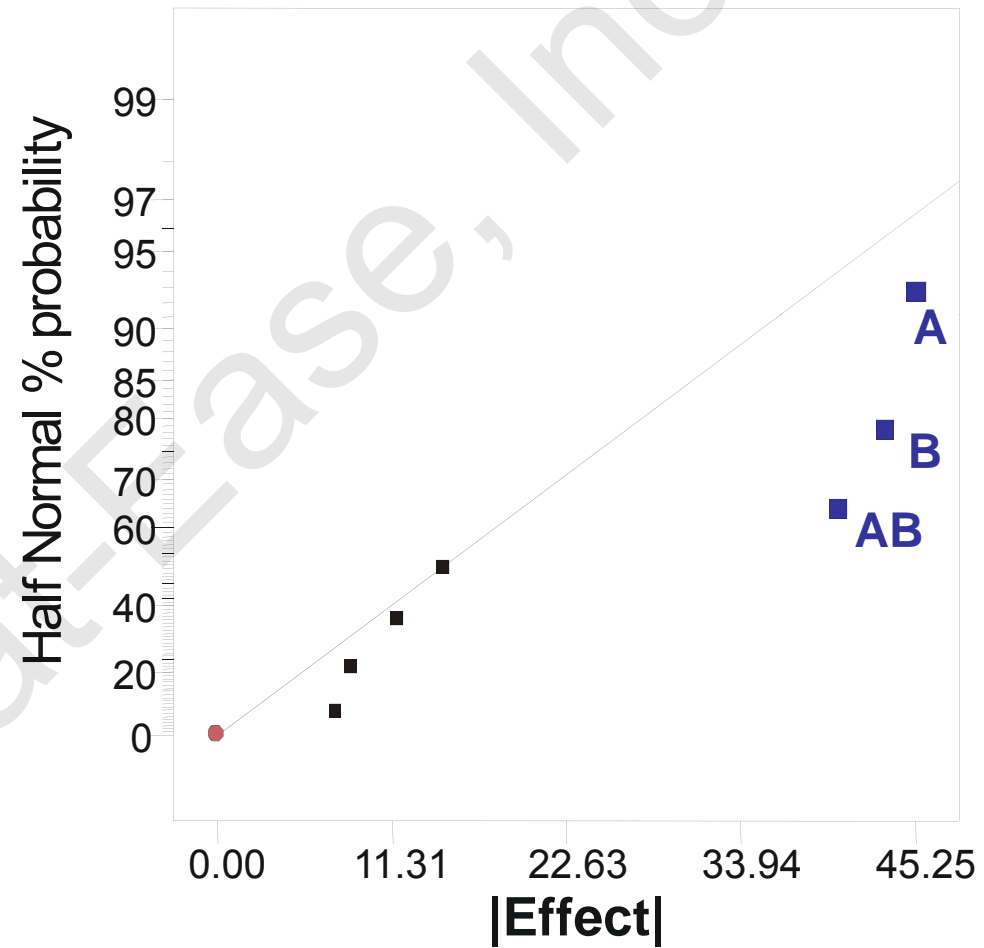


Box's protégé makes bearing breakthrough, but is it too good to be true?



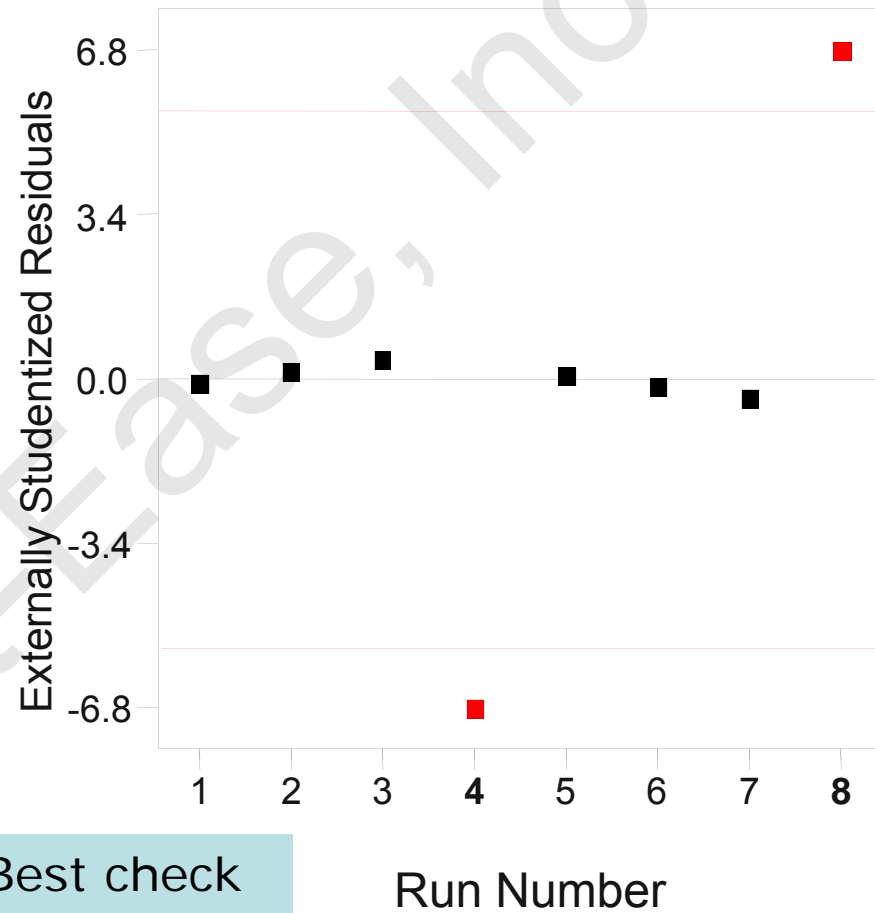
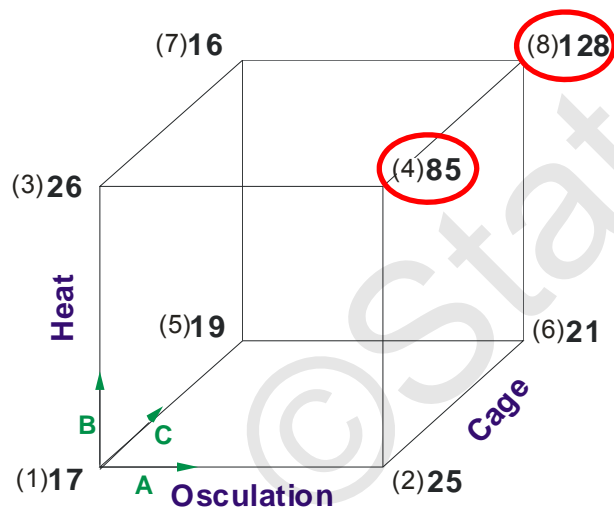
# Bearing Case: Half-Normal Plot of Effects

*What's wrong  
with this  
picture?*



# Bearing Case: Apparent Outliers

*Toss the outliers?  
Better check  
first to identify  
them (see cube  
plot for run #'s).*

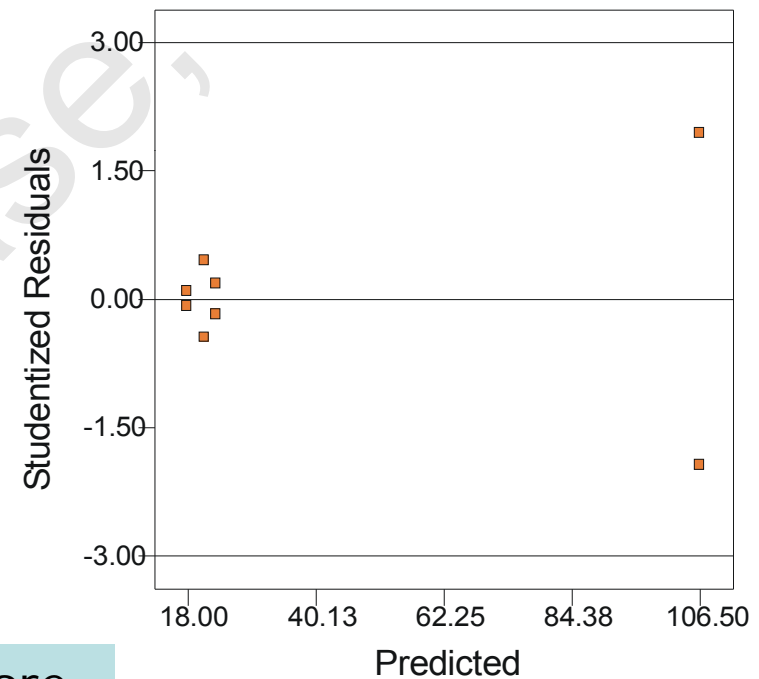
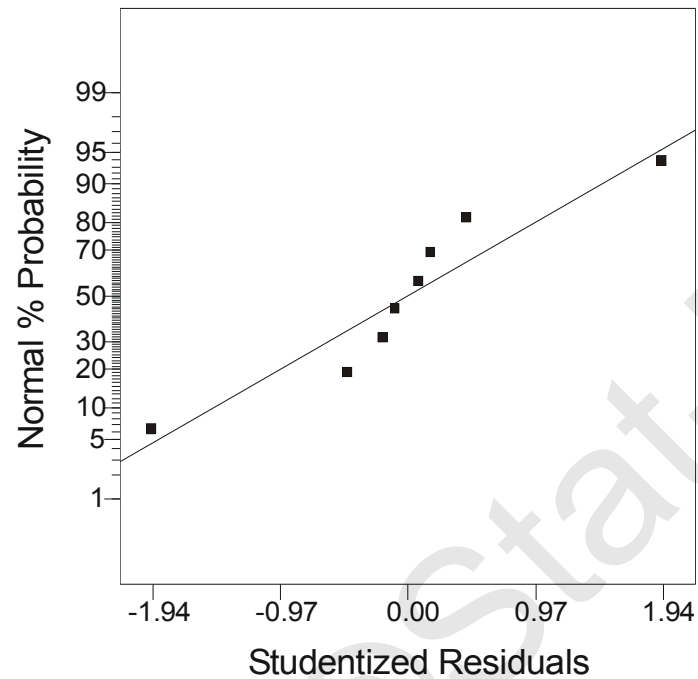


Best check  
diagnostics!



## Bearing Case: Further Diagnostics

*Is assumption correct that residuals are normally distributed with constant variance?*



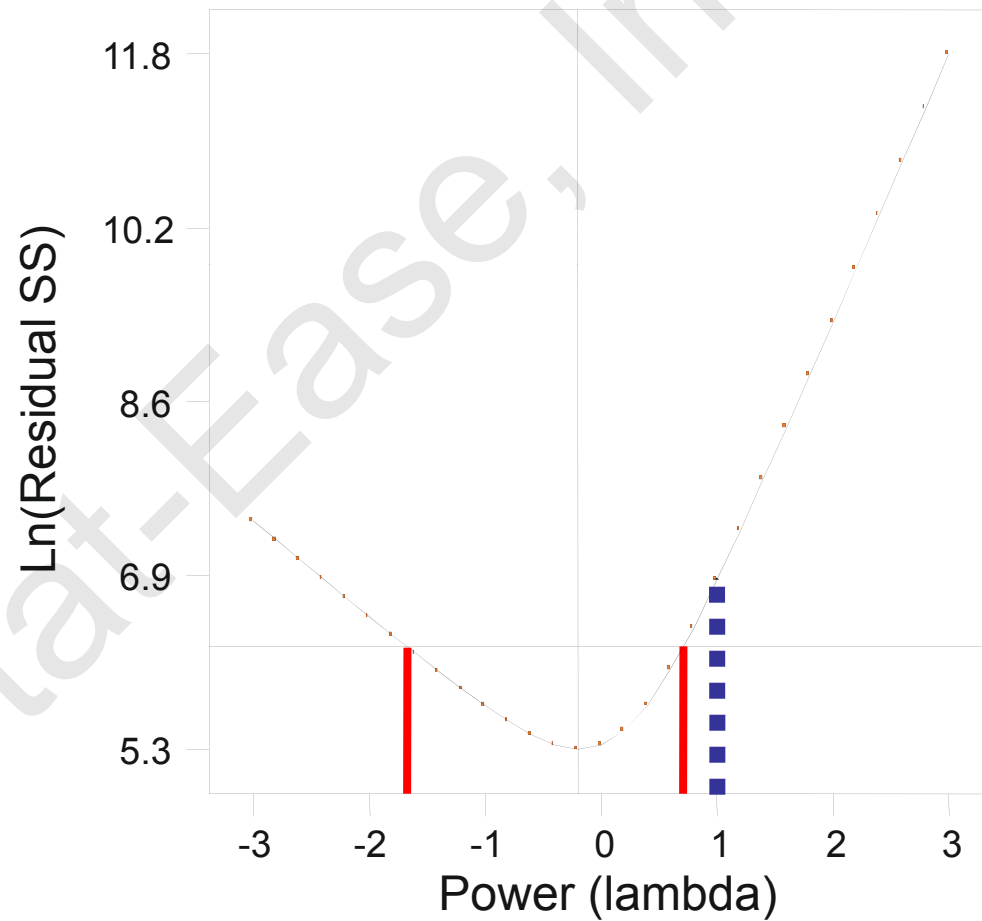
One more  
diagnostic!



## Bearing Case: Box-Cox Plot

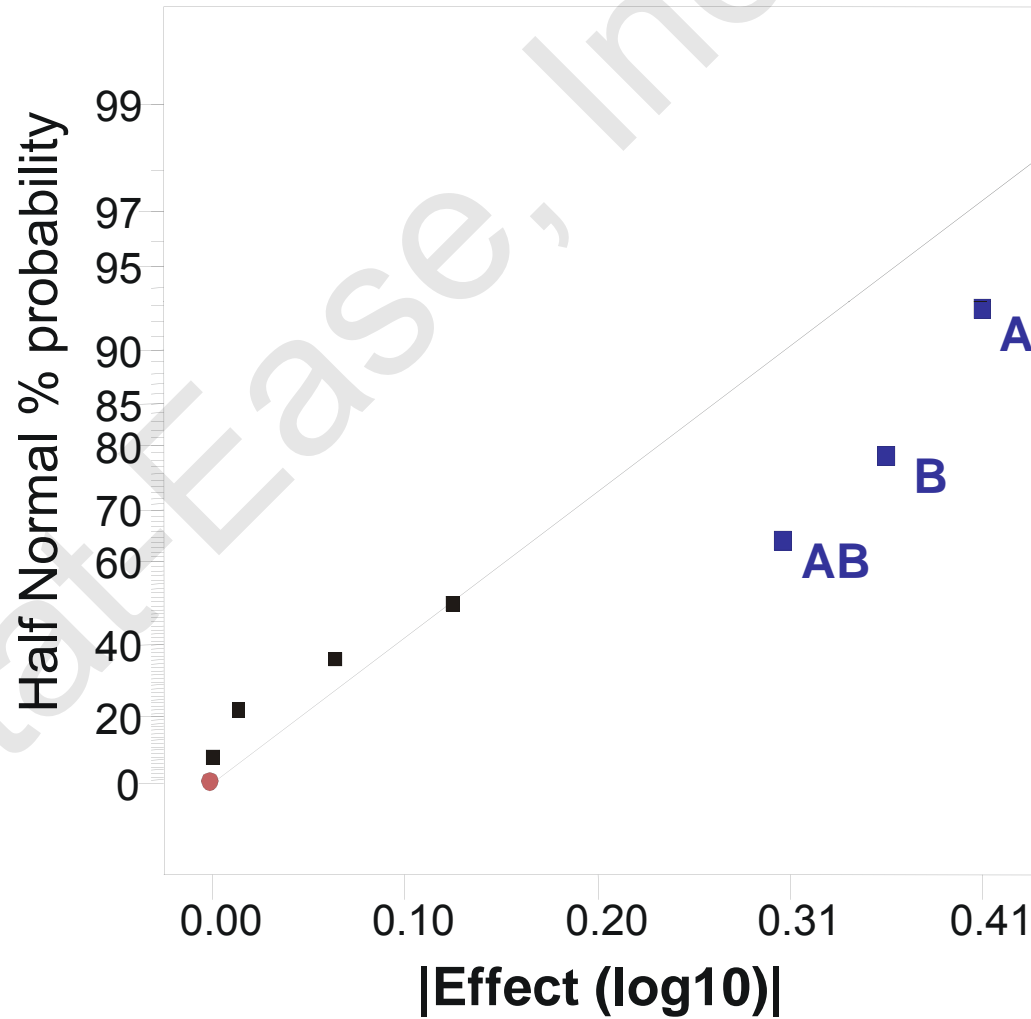
*Blue line is  
outside of  
red zone.*

*☞ Transform  
will help -  
try log.*



# Bearing Case (after *log* transformation): Plot of Effects

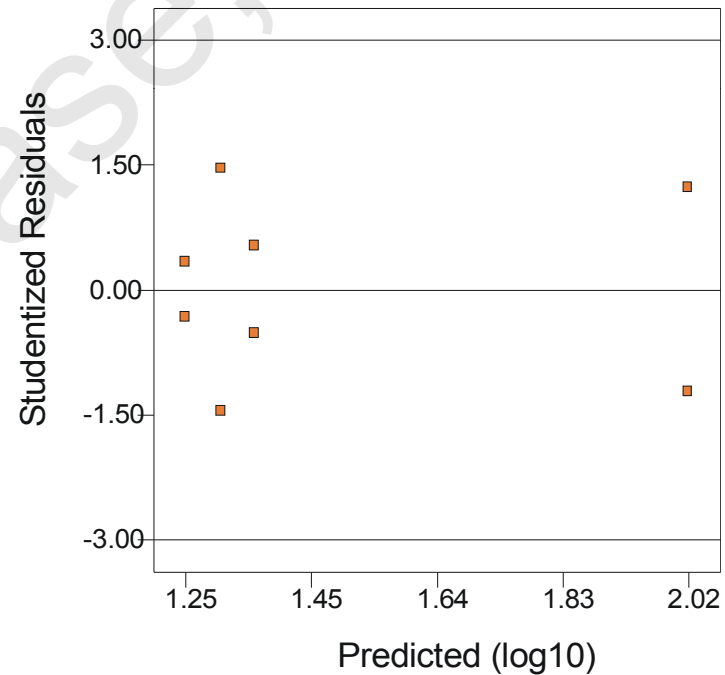
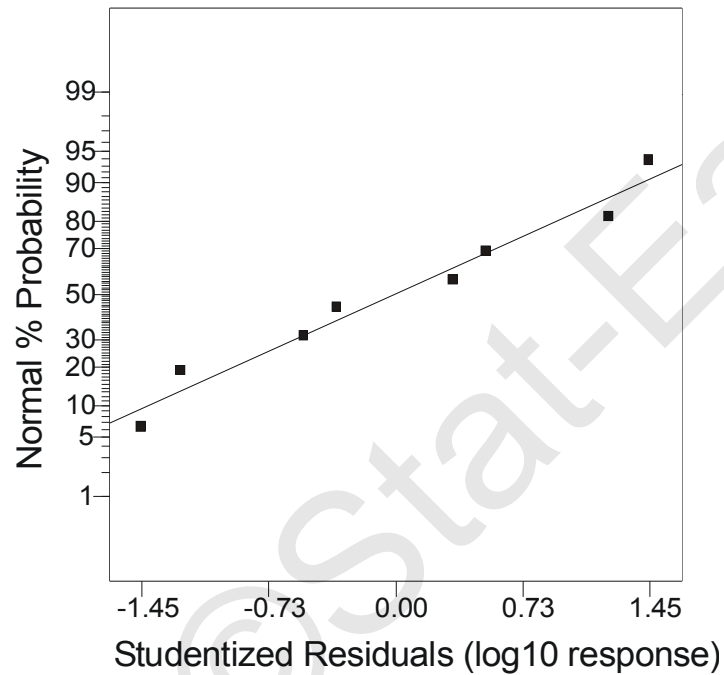
*Nice line-up!*





# Bearing Case (after *log* transformation): Residual Diagnostic Plots

*Normally distributed with constant variance!*



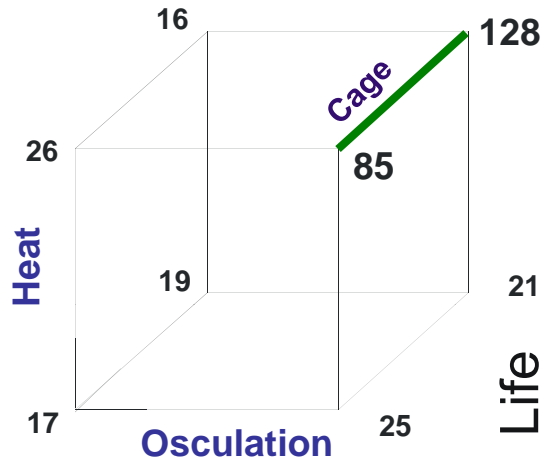
## Bearing Case (after *log* transformation): Plot for Detecting Outliers

*Can include  
the fabulous  
results! None  
are outliers.*

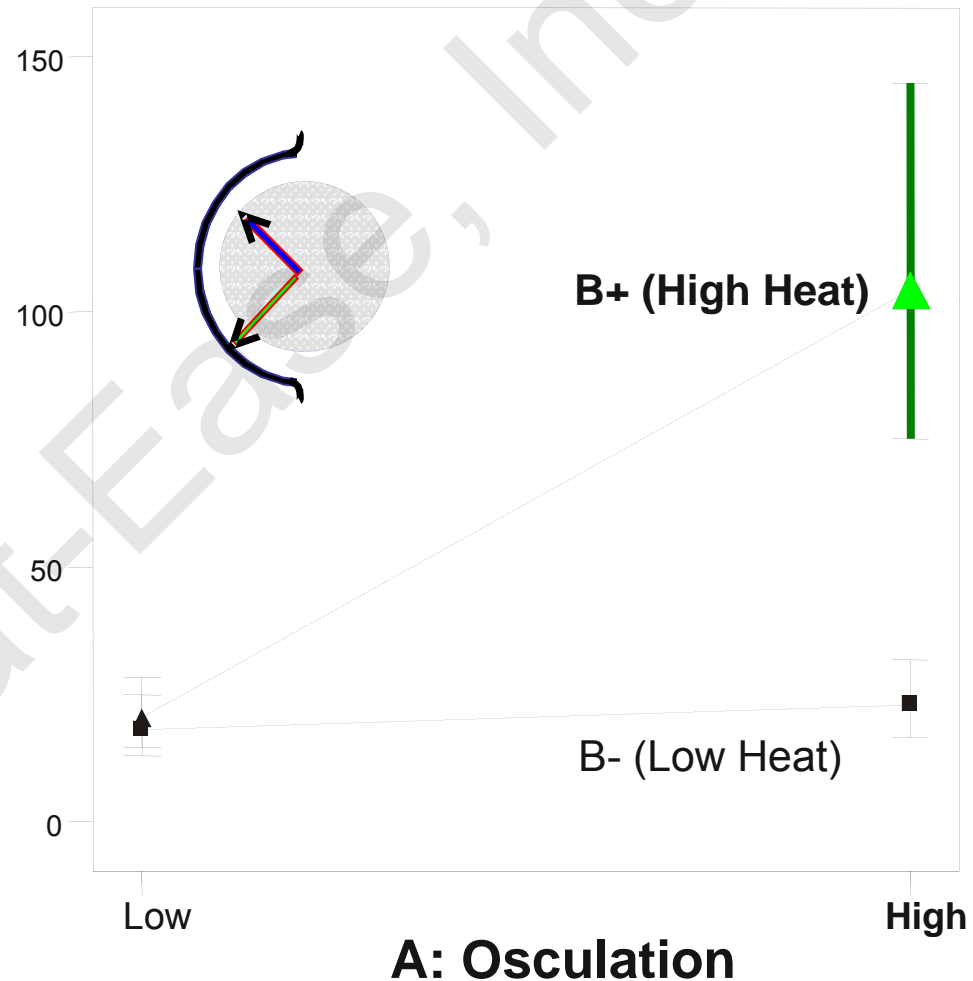


*"Nature goes her own way and all that seems an  
exception is really according to order."  
-- Goethe*

# Bearing Case (after *log* transformation): Interaction Plot (the happy ending!)



Notice how confidence (LSD) bar widens at breakthrough conditions.



## The rest of the story



Swedish manufacturer SKF invented roller bearings in 1919, but by the '70s the Japanese had achieved comparable quality at competitive prices. These pressures inspired SKF engineers\* to quit doing experiments only one factor at a time and try a two-level factorial design (led by Box' protégé).

Ultimately SKF improved their actual bearing life from 41 million revolutions on average (already better than any competitors), to 400 million revs\* – nearly a ten-fold improvement!

\*("Breaking the Boundaries," *Design Engineering*, Feb 2000, pp 37-38.)

## Recap of this case via Design-Expert® Software

Design-Expert makes it easy to set up this experiment design, model the results and analyze them statistically—including diagnosing the residuals, which in this case proves to be of vital importance.



*Bearings*



- ✓ *Thorny issues (stuff happens)*
- ✓ *The secret to long life (bearing case)*
- ❑ A case to test your metal (defects defeated!)
- ❑ Conclusions

# A Case to Test Your Metal



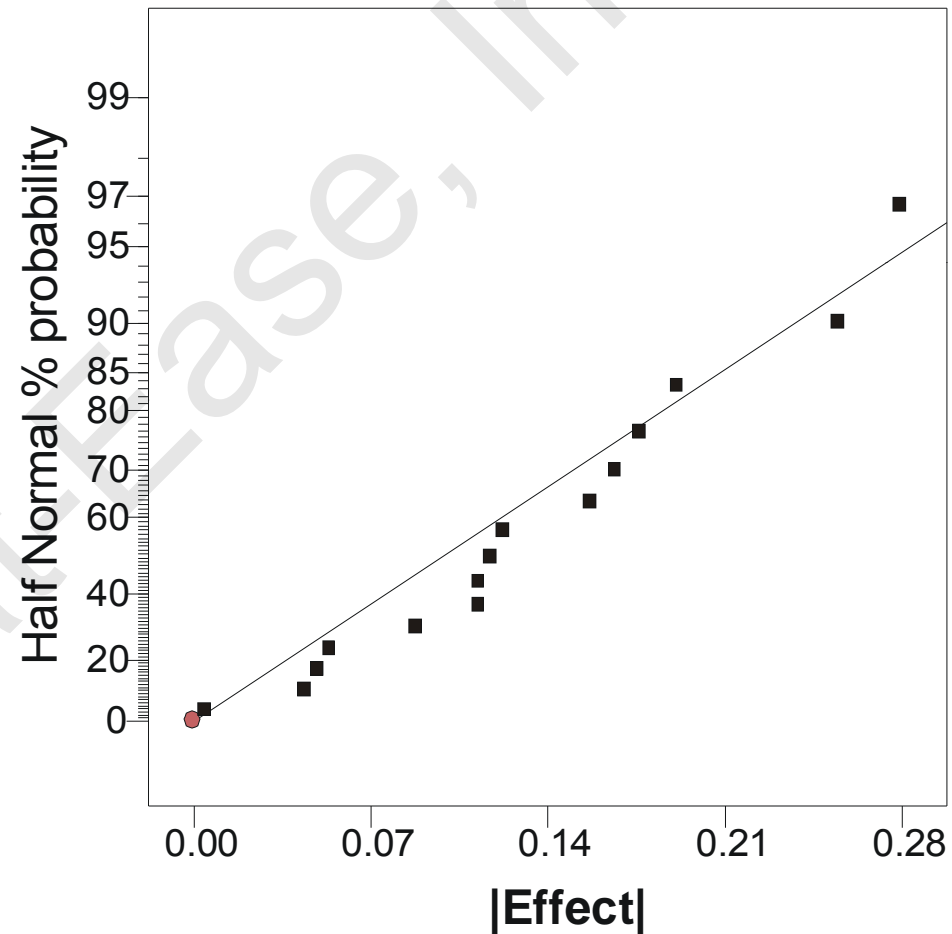
Defect rates on die-cast aluminum disk-drive housing drop dramatically, but is it real?

Std	A Oil Temp	B Trip	C Metal Temp	D Shot	E Dwell	Fraction Defect
1	350	390	1260	1.60	5.50	0.14
2	450	390	1260	1.60	3.50	0.98
3	350	410	1260	1.60	3.50	0.36
4	450	410	1260	1.60	5.50	0.42
5	350	390	1300	1.60	3.50	1.00
6	450	390	1300	1.60	5.50	0.90
7	350	410	1300	1.60	5.50	0.28
8	450	410	1300	1.60	3.50	0.14
9	350	390	1260	2.20	3.50	0.22
10	450	390	1260	2.20	5.50	0.26
11	350	410	1260	2.20	5.50	0.38
12	450	410	1260	2.20	3.50	0.12
13	350	390	1300	2.20	5.50	0.30
14	450	390	1300	2.20	3.50	0.06
15	350	410	1300	2.20	3.50	0.22
16	450	410	1300	2.20	5.50	0.38

## A Case to Test Your Metal Normal Plot of Effects

All effects line up  
so evidently  
nothing is  
significant. ☹️

Don't give up yet  
– try transform:  
arc-sin square  
root good for  
binomial data  
like this.



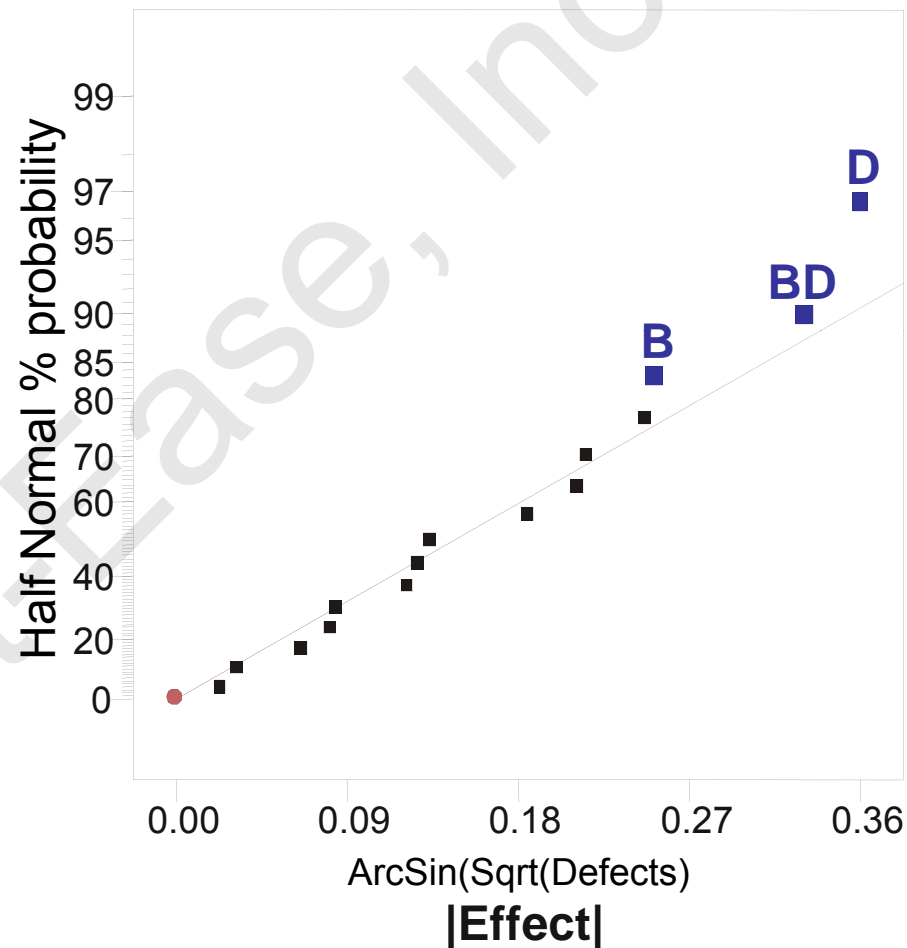


# A Case to Test Your Metal

## Normal Plot of Effects (*transformed*)

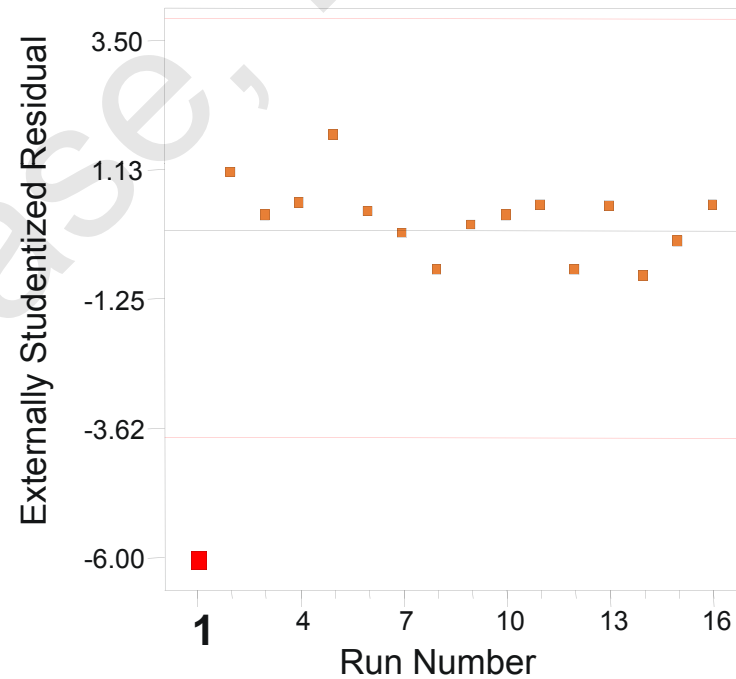
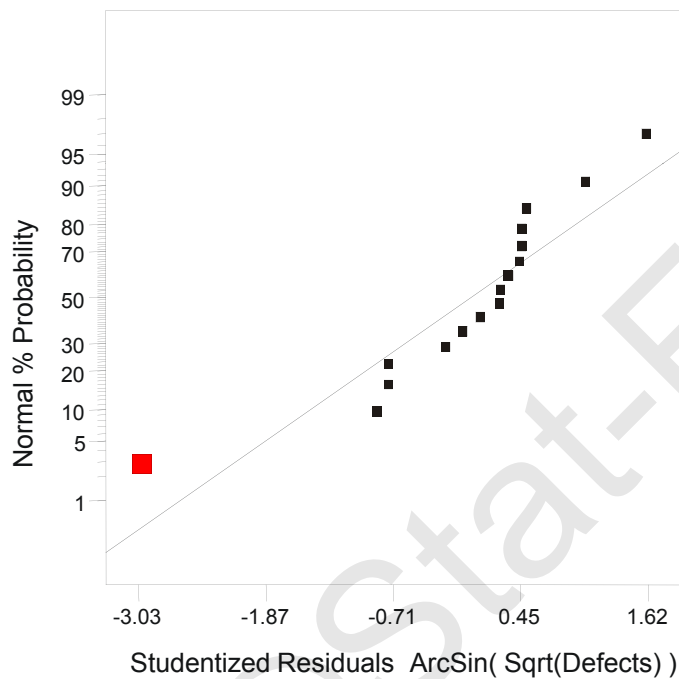
All effects still line up so arc-sin square root no help. ☹ ☹

Don't give up yet – pick several of the biggest effects and look for outliers.



# A Case to Test Your Metal Diagnostic Plots

Problem revealed: Obvious outlier! Special cause?



## A Case to Test Your Metal Investigation of Outlier

Diagnostic plots identified standard order number 1 as a discrepant outcome. The foreman, when confronted with this statistical evidence, broke down and confessed that his crew overlooked this particular combination of factors. They then tried to make up for it by coming in early the following week, after shutting down the foundry over the weekend, to sneak the missing run in before the engineer came in to work.



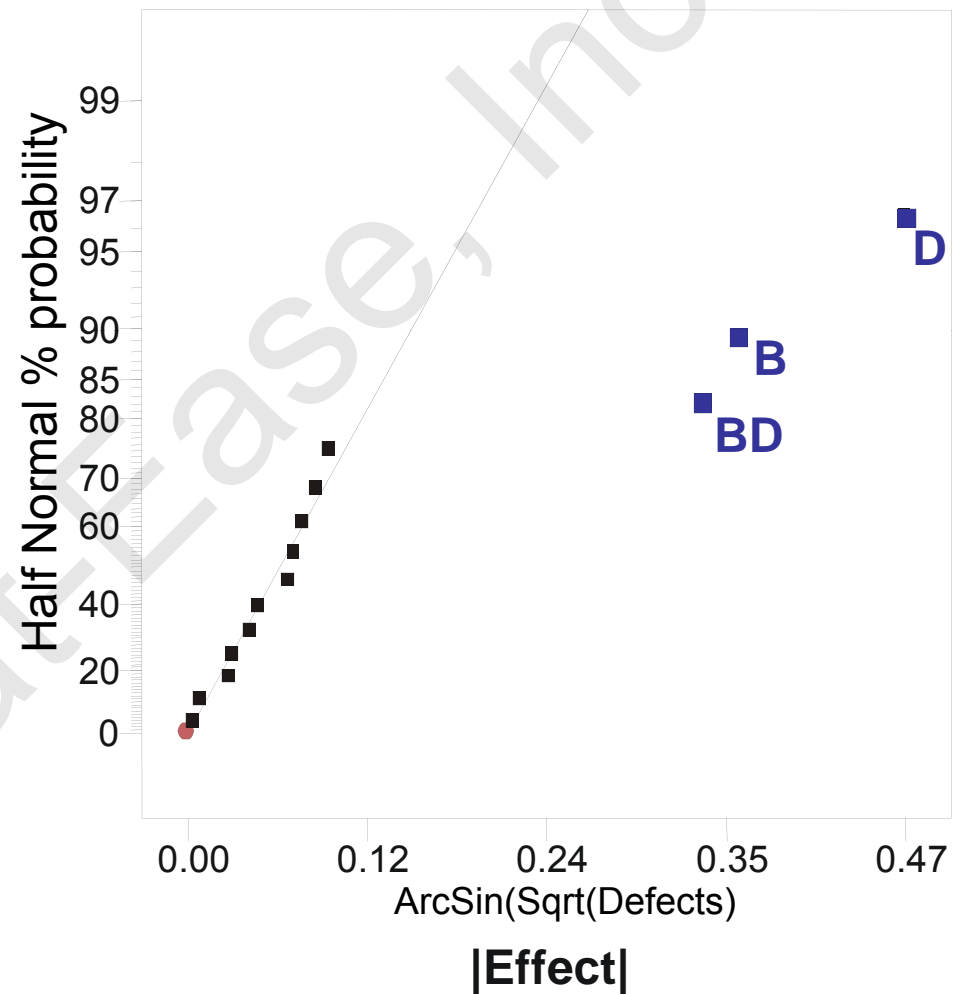
*Next step: ignore this run and re-analyze.*

# A Case to Test Your Metal (*outlier removed*)

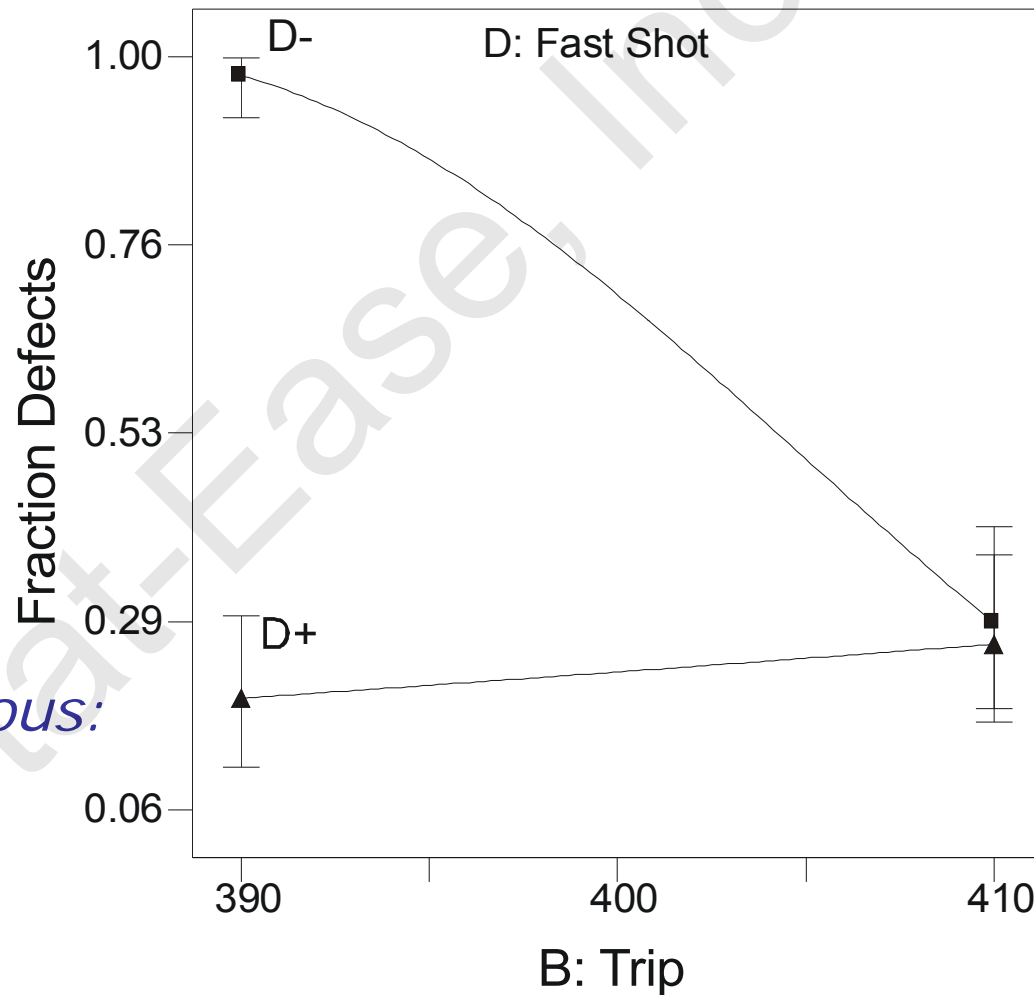
## Normal Plot of Effects

Family of effects  
now clearly  
significant. 😊

*(Warning: missing  
data causes  
information loss,  
but not serious  
in this case.)*



# A Case to Test Your Metal (*outlier removed*) Interaction Plot (*the happy ending!*)



*Answer now obvious:  
Do not run both  
B & D low.*

## Recap of this case via Design-Expert® Software

Again, Design-Expert makes it easy to set up this experiment design, model the results and analyze them statistically—including diagnosing the residuals, which, as in the last case, proves to be of vital importance.



*metmold-outlier ignored*



- ✓ *Thorny issues (stuff happens)*
- ✓ *The secret to long life (bearing case)*
- ✓ *A case to test your metal (defects defeated!)*
- Conclusions

An outlier is a response from an experiment that does not fit the proposed model. Before jumping to any conclusions, consider these possibilities:

1. The model is faulty, not the data (*Ex. bearing case*).
  - Watch for bad patterns on diagnostic plots: normal, residuals versus predicted, outlier (externally studentized) and Box-Cox.
  - Try transformation such as a log, square root (for counts), inverse (for rates) or arcsin square root (for fraction defects).



2. The result really is an outlier (*Ex. die-cast aluminum*).
  - Look for possible errors in data entry, or in response measurement, or in the conduct of that particular experimental run.
  - If the response really differs at that particular combination of the design factors, further study may lead to an important discovery!

*Above all – avoid bias:*

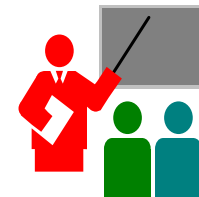
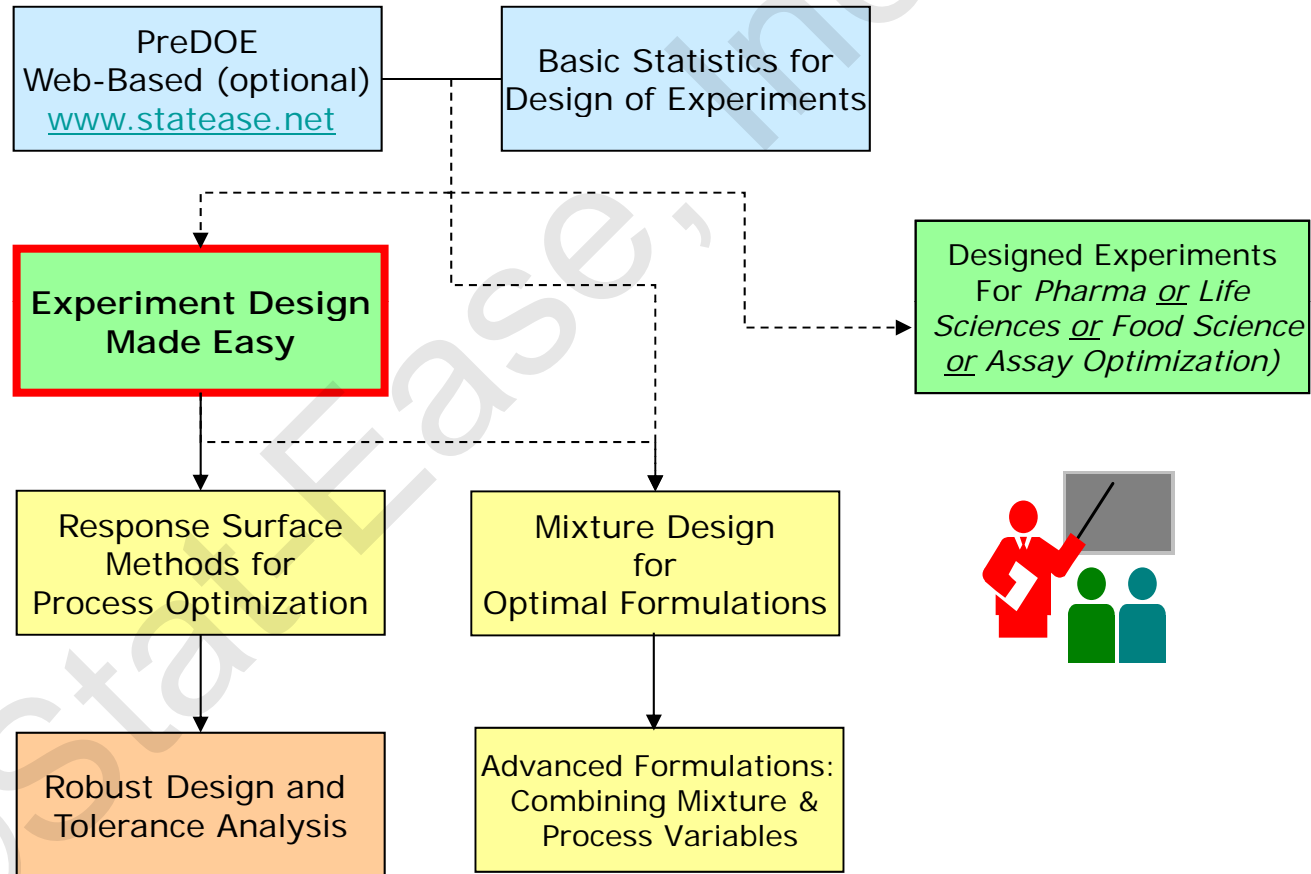
*“The first principle is that you must not fool yourself--and you are the easiest person to fool.”*

*- Richard Feynman*

# Stat-Ease Training: Computer-Intensive Statistical Workshops



Shari Kraber,  
Workshop Manager  
& Master Statistician  
[shari@statease.com](mailto:shari@statease.com)



# How to get help



- ❑ Search publications posted at [www.stateease.com](http://www.stateease.com).
- ❑ In Stat-Ease software press for Screen Tips, view reports in annotated mode, look for context-sensitive Help (right-click) or search the main Help system.
- ❑ Explore Experiment Design Forum <http://forum.stateease.com> and post your question (if not previously answered).
- ❑ E-mail [stathelp@stateease.com](mailto:stathelp@stateease.com) for answers from Stat-Ease's staff of statistical consultants.
- ❑ Call 612.378.9449 and ask for "statistical help."



# Statistics Made Easy®



*Best of luck for your  
experimenting!*

*Thanks for listening!*

*-- Mark*

Mark J. Anderson, PE, CQE  
Stat-Ease, Inc.  
[mark@statease.com](mailto:mark@statease.com)

*\*Pdf of this Powerpoint presentation posted at [www.statease.com/webinar.html](http://www.statease.com/webinar.html).  
For future webinars, subscribe to DOE FAQ Alert at  
[www.statease.com/doealert.html](http://www.statease.com/doealert.html).*